In the name of God

## Department of Physics Shahid Beheshti University

## ADVANCED TOPICS IN STATISTICAL PHYSICS II

## Exercise Set 7

## (Date Due: 1395/04/10)

1. Computational program: Here we are going to compute Kramers-Moyal coefficients for simulated data given in previous set of problem.

**A**: Compute  $D^{(1)}(x,t)$  and  $D^{(2)}(x,t)$  and plot them as a function of x. (Hint: at first you should determine the markov length scale and set  $t = t_{Markov}$ .)

**B**: Show that  $D^{(4)}(x,t)$  is very small in comparison with  $D^{(2)}(x,t)$ .

**2.** According to forward solution, and suppose that  $D^{(4)}(x,t) = 0$ , show that:

$$p(x,t+\tau|x',t) = \left[1 - \frac{\partial}{\partial x}D^{(1)}(x,t)\tau + \frac{\partial^2}{\partial x^2}D^{(2)}(x,t)\tau\right]\delta(x-x')$$

has the following solutions:

 $\mathbf{A}$  :

$$p(x,t+\tau|x',t) = \frac{1}{2\sqrt{\pi D^{(2)}(x',t)\tau}} \exp\left(-\frac{[x-x'-D^{(1)}(x',t)\tau]^2}{4D^{(2)}(x',t)\tau}\right)$$

 $\mathbf{B}$  :

$$p(x,t+\tau|x',t) = \frac{1}{2\sqrt{\pi D^{(2)}(x,t)\tau}} \exp\left(-\frac{\partial}{\partial x}D^{(1)}(x,t)\tau + \frac{\partial^2}{\partial x^2}D^{(2)}(x,t)\tau - \frac{[x-x'-(D^{(1)}(x,t)-2\frac{\partial}{\partial x}D^{(2)}(x,t))\tau]^2}{4D^{(2)}(x,t)\tau}\right)$$

Good luck, Movahed