

In the name of God

Department of Physics  
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COMPUTATIONAL PHYSICS

Exercise Set 5

(Date Due: 1395/02/05)

1. For cooling differential equation, calculate analytical solution as well as numerical one. Then plot  $\Delta$  as a function of discretization parameter.
2. Compute Temperature profile for position and time for a rod.
3. Solve Laplace's equation numerically. (relaxation method or finite difference method)
4. Solve the following integration numerically:

$$\langle v_z^2 \rangle = \int_{-\infty}^{+\infty} dv_x \int_{-\infty}^{+\infty} dv_y \int_{-\infty}^{+\infty} dv_z v_z^2 p_v(\vec{v})$$

here  $p_v(\vec{v}) = \left(\frac{\beta m}{2\pi}\right)^{3/2} \exp\left(-\frac{\beta m \vec{v}^2}{2}\right)$ . You can imagine any values for free parameters.

5. Write down a program to compute the rounding errors of your computer for single and double precisions.
6. Using Euler and RF4 methods, solve following initial value problem:

$$y''(t) + ay'(t) + \omega^2 y(t) = \cos(\omega_1 t)$$

with  $y(0) = A$ ,  $y'(0) = 0$  and take any arbitrary values for other free parameters.

Good luck, Movahed

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